

# Apathy is the Root of all Expressions

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## HOSVD-based Face Models

- 3D face scan database with sparse correspondences [15]
- Compute full correspondences [16]
- Arrange into tensor and subtract mean shape  
 $\mathcal{T} = \mathcal{T}_{\text{orig}} - \mathcal{T}_0 \in \mathbb{R}^{3N \times P \times E}$
- Compute HOSVD  
 $\mathcal{T} \approx \hat{\mathcal{T}} = \mathcal{S} \times_1 \mathbf{U}^{(1)} \times_2 \mathbf{U}^{(2)} \times_3 \mathbf{U}^{(3)}$
- 3D shape represented as sum of mean  $\mathbf{m}$  and mean-free shape  
 $\hat{\mathbf{s}}^{3D} = \mathbf{m} + \hat{\mathbf{v}} \in \mathbb{R}^{3N}$

Mean-free shape  $\hat{\mathbf{v}}$  can be described using different models.

### 1. Model: Baseline Model

$$\hat{\mathbf{v}}(\mathbf{u}_2, \mathbf{u}_3) = \mathcal{S} \times_1 \mathbf{U}^{(1)} \times_2 \mathbf{u}_2^T \times_3 \mathbf{u}_3^T, \quad \mathbf{u}_2 \in \mathbb{R}^{L_2}, \quad \mathbf{u}_3 \in \mathbb{R}^{L_3}$$

### 2. Model: Substructure-aware Model (proposed-1)

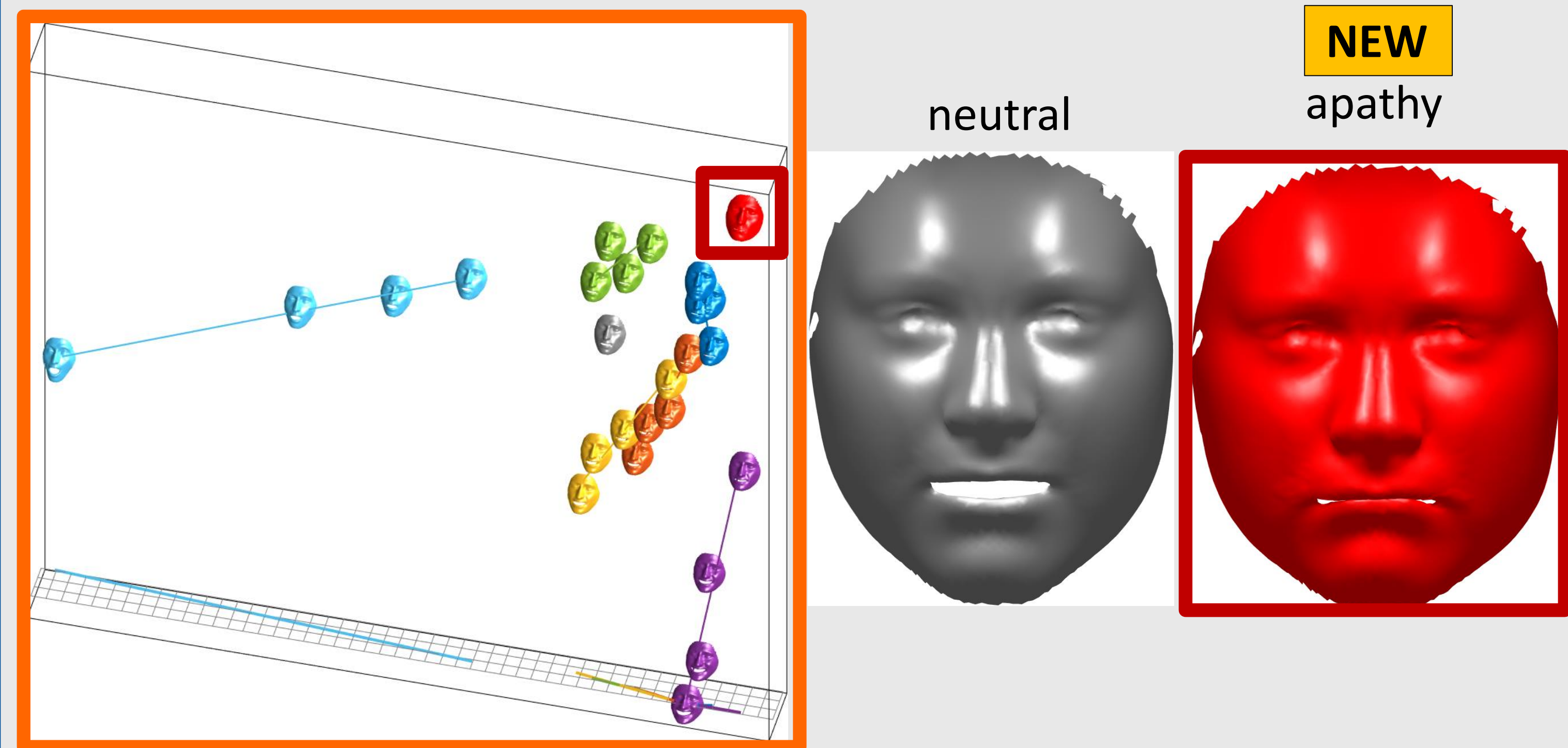
$$\hat{\mathbf{v}}(\mathbf{p}_2, \mathbf{p}_3) = \mathcal{S} \times_1 \mathbf{U}^{(1)} \times_2 \mathbf{p}_2^T \mathbf{U}^{(2)} \times_3 \mathbf{p}_3^T \mathbf{U}^{(3)}, \quad \mathbf{p}_2 \in \mathbb{R}^P, \quad \mathbf{p}_3 \in \mathbb{R}^E$$

### 3. Model: ICA-based Model (proposed-2)

$$\hat{\mathbf{v}}(\mathbf{p}_2, \mathbf{b}_3) = \mathcal{S} \times_1 \mathbf{U}^{(1)} \times_2 \mathbf{p}_2^T \mathbf{U}^{(2)} \times_3 (\mathbf{b}_3^T \mathbf{B} + \mathbf{a}_0^T), \quad \mathbf{p}_2 \in \mathbb{R}^P, \quad \mathbf{b}_3 \in \mathbb{R}^3$$

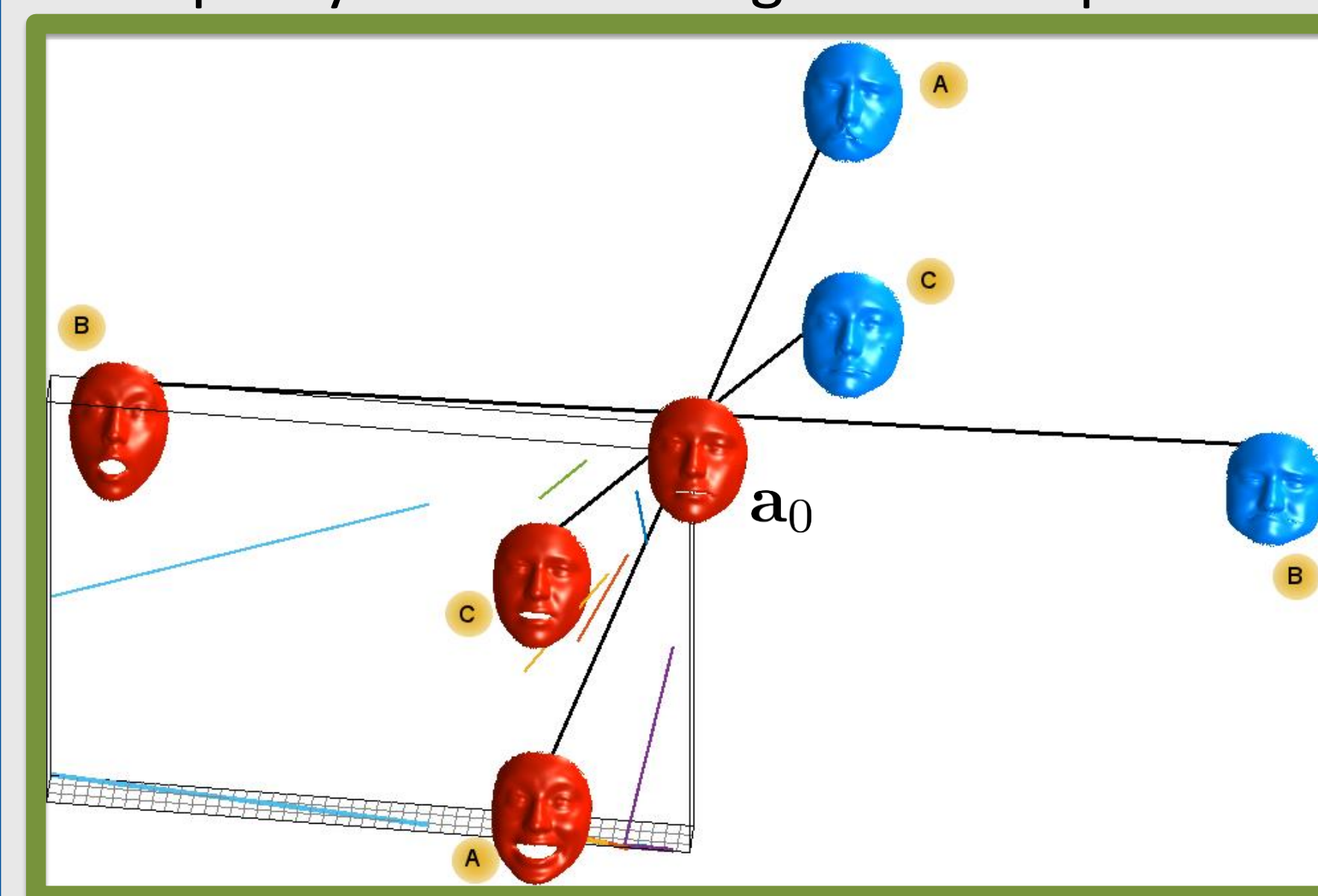
	Model 1	Model 2	Model 3
Takes use of person and expression space $\mathbf{U}^{(k)}$	✗	✓	✓
Canonical basis of parameter vectors	✗	✓	✓
Incorporate low-dimensional substructure $\mathbf{U}^{(3)}$	✗	✗	✓
Robust person and expression transfer	✗	✓	✓
Number of expression parameters	$L_3 \leq E$	$E = 25$	3

## Substructure of Expression Space



First three dimensions of expression space  $\mathbf{U}^{(3)}$

- Each emotion displayed in one color approximates one line.
- Expressions form a planar substructure.
- Lines intersect in new „apathetic“ expression (not part of database).
- Apathy as natural origin of all expressions.



### Reduced expression space:

Compute ICA on apathy-centred expression space to receive 3 projection pursuit directions and thereby new basis expressions. Note that these lie in the plane, but partly outside the training data (blue).

## Applications

### Person and Expression Transfer

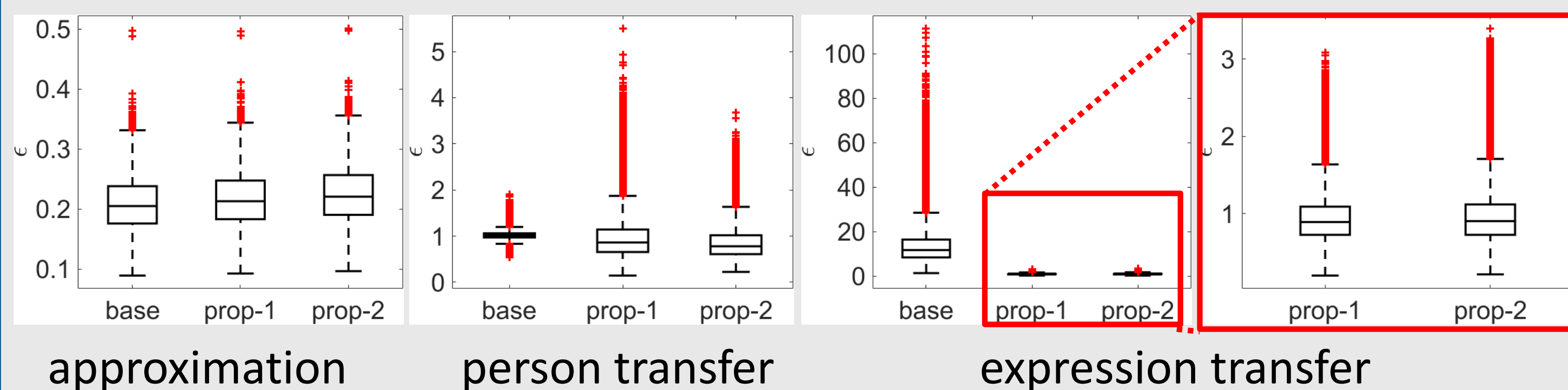
How robust can person and expression transfer be done?

- Exclude expression (or person) from data tensor
- Re-estimate model
- Estimate model parameters for remaining faces for each model

$$\min \|\hat{\mathbf{v}} - \mathbf{v}\|_2^2 + \lambda_1 \|\mathbf{p}_2\|_2^2 + \lambda_2 \|\mathbf{p}_2^T \mathbf{1} - 1\|_2^2 + \lambda_3 \|\mathbf{p}_3\|_2^2 + \lambda_4 \|\mathbf{p}_3^T \mathbf{1} - 1\|_2^2$$

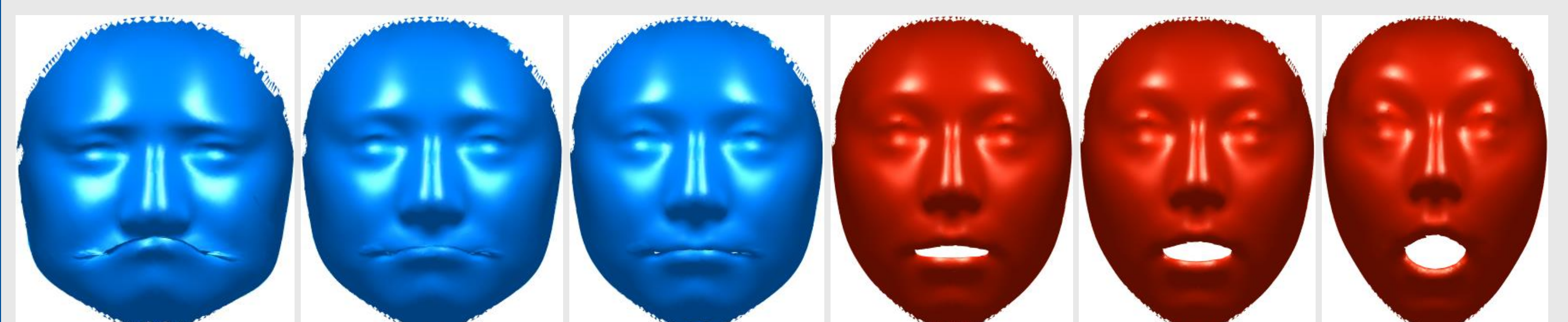
- Change expression (or person) parameters to known values

- Compute error  $\epsilon = \frac{\|\hat{\mathbf{v}} - \mathbf{v}_{\text{true}}\|_2}{\|\mathbf{v}_{\text{true}}\|_2}$

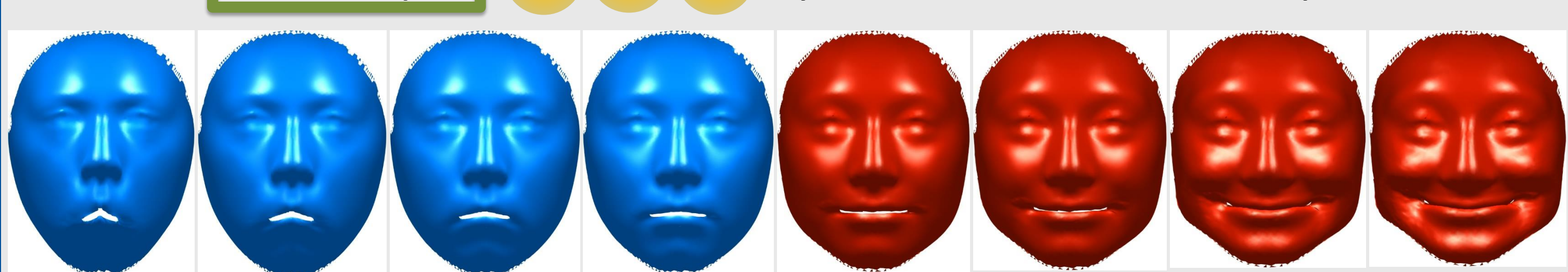


### Synthesis of Expression Trajectories

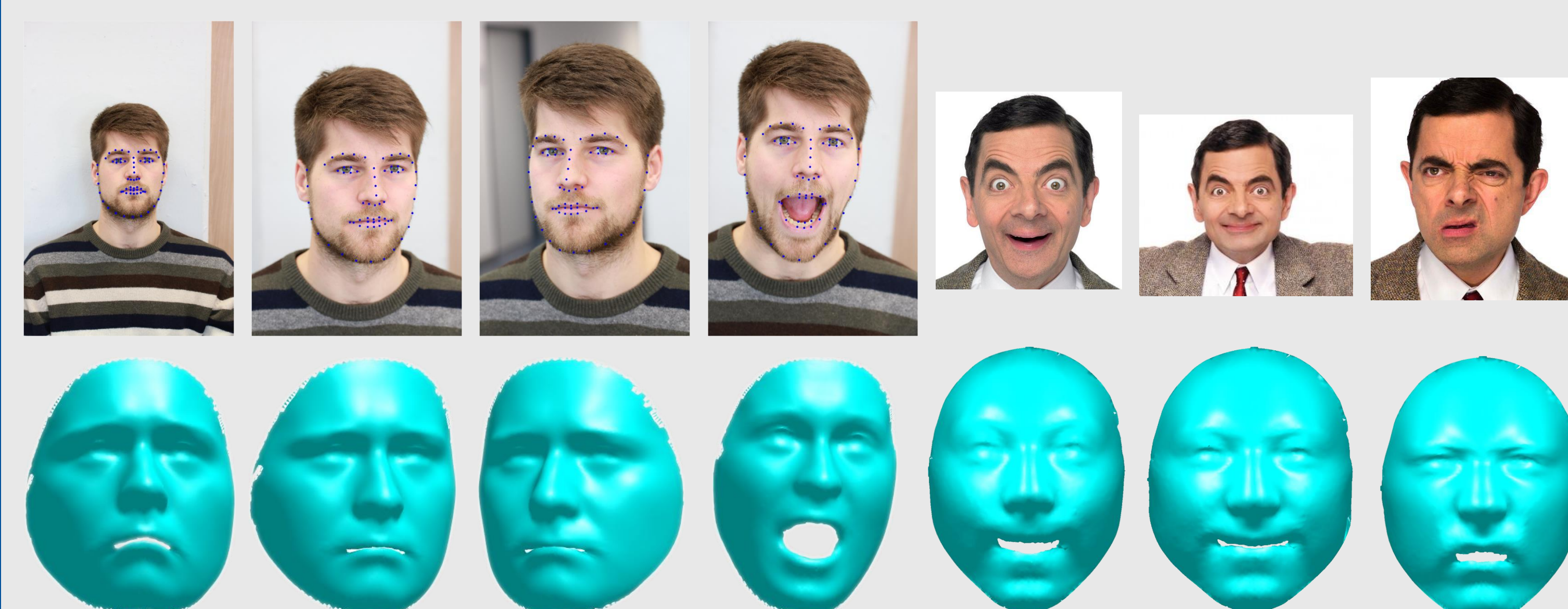
Example expression trajectory based on direction **B** with weight values -1, -0.5, -0.25, 0.25, 0.5, 1



Based on **basis shapes A, B, C**, synthesize new unseen expressions:



### 3D Reconstruction from Sparse Landmarks



### Emotion Classification

- Exclude person from data tensor
- Re-estimate model
- Estimate parameters for person and expression excluded persons
- Assign one of the 7 emotions based on *k*-nearest-centroid (*kNC*) classification

**Classification Rate:**

**Model 1 : 15%**

**Model 3 : 60%**